



# Dalitz Plot Analysis of $B \rightarrow DDK$ decays

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*for the BaBar collaboration*

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# Introduction

- Results recently published by BaBar (March 2015)
- Analysis chiefly done by Vincent Poireau (LAPP, Annecy)

PHYSICAL REVIEW D 91, 052002 (2015)

Dalitz plot analyses of  $B^0 \rightarrow D^- D^0 K^+$  and  $B^+ \rightarrow \bar{D}^0 D^0 K^+$  decays

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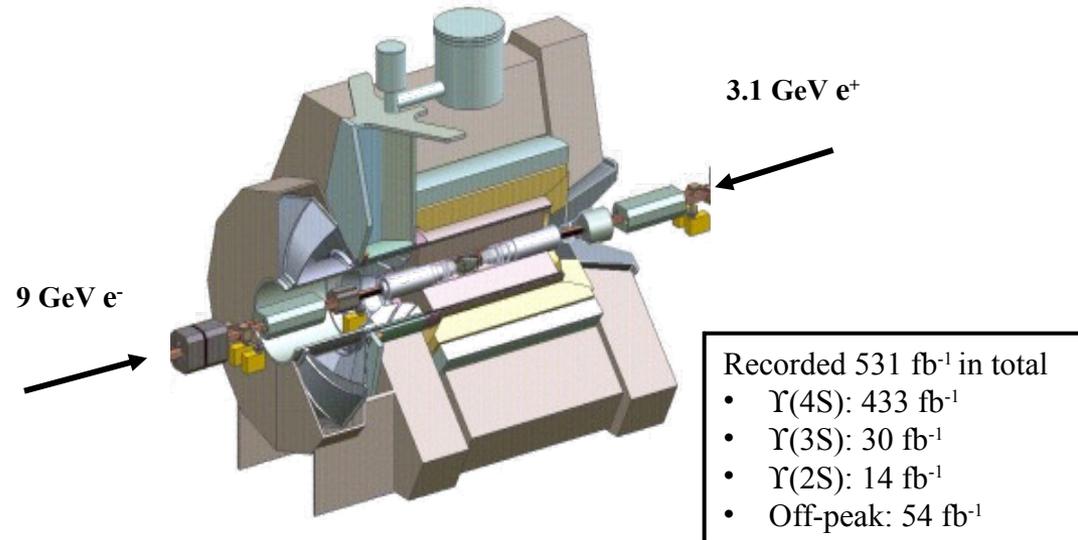
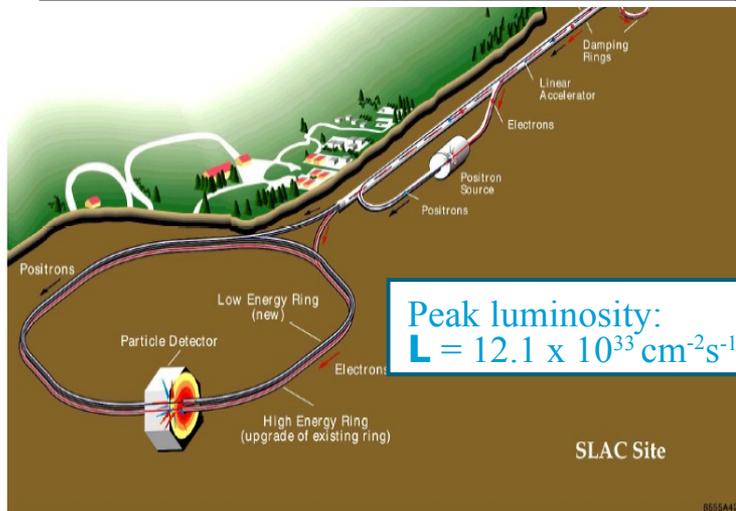
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# Introduction, continued

Center of mass: 10.58 GeV  
 $e^+ e^- \rightarrow \Upsilon(4S) (b\bar{b}) \rightarrow B\bar{B}$



- The *BABAR* experiment switched off in 2008, but still produces many interesting results!

- 549 papers in total
- 26 in 2013
- 15 in 2014
- ~15 expected in 2015

# Introduction, continued

- Studying  $B \rightarrow D^{(*)}D^{(*)}K$  decays

- **22 modes**

- These modes have been the topics of **three previous BaBar papers**

- Time-dependent  $CP$  asymmetry in  $B \rightarrow D^{*-}D^{*+}K^0_S$  Phys. Rev. D74, 091101, 2006
- Study of the resonances  $\psi(3770)$ ,  $D_{s1}(2536)$ , and  $X(3872)$  Phys. Rev. D77, 011102, 2008
- Measurement of 22 **branching fractions** Phys. Rev. D83, 032004, 2011

- These decays contain **resonances**

in  $D^{(*)}D^{(*)}K$  ( $c\bar{s}$ ) or

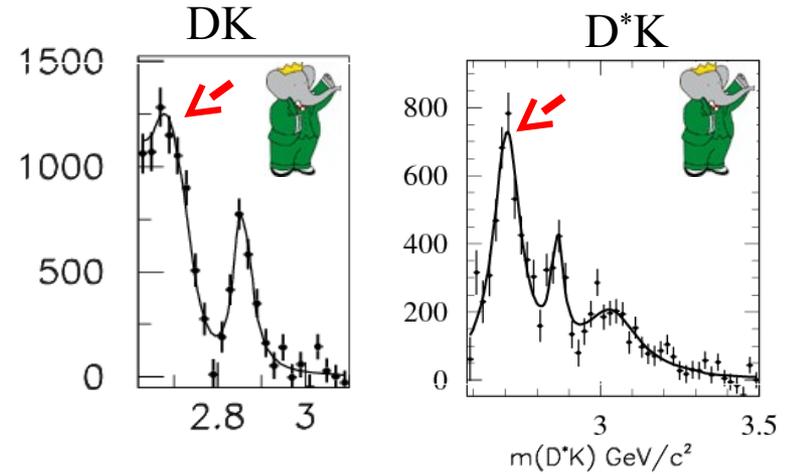
$D^{(*)}D^{(*)}K$  ( $c\bar{c}$ )

- Here we report on properties of the  $D_{s1}(2700)$

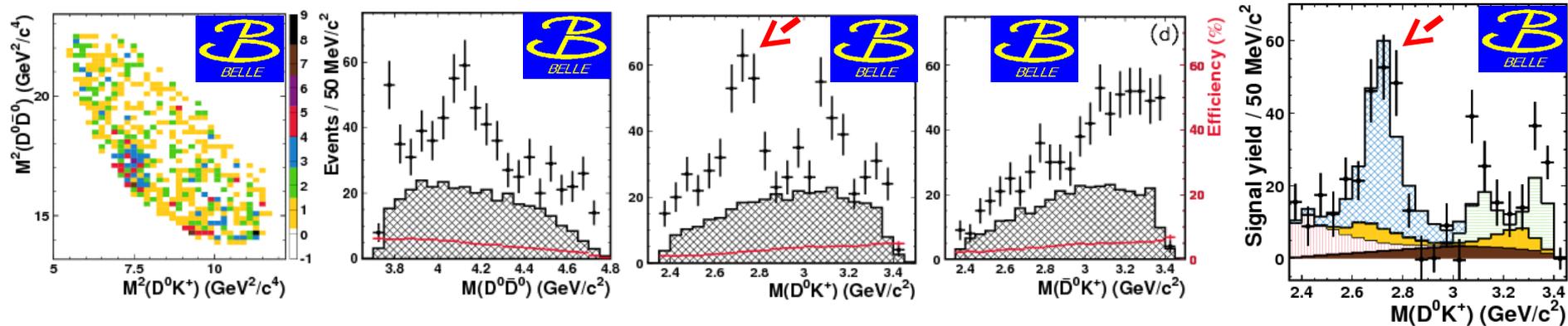
Neutral $B$ mode	Charged $B$ mode
$B^0 \rightarrow D^- D^0 K^+$	$B^+ \rightarrow \bar{D}^0 D^+ K^0$
$B^0 \rightarrow D^- D^{*0} K^+$	$B^+ \rightarrow \bar{D}^0 D^{*+} K^0$
$B^0 \rightarrow D^{*-} D^0 K^+$	$B^+ \rightarrow \bar{D}^{*0} D^+ K^0$
$B^0 \rightarrow D^{*-} D^{*0} K^+$	$B^+ \rightarrow \bar{D}^{*0} D^{*+} K^0$
$B^0 \rightarrow D^- D^+ K^0$	$B^+ \rightarrow \bar{D}^0 D^0 K^+$
$B^0 \rightarrow D^- D^{*+} K^0 + D^{*-} D^+ K^0$	$B^+ \rightarrow \bar{D}^0 D^{*0} K^+$
	$B^+ \rightarrow \bar{D}^{*0} D^0 K^+$
$B^0 \rightarrow D^{*-} D^{*+} K^0$	$B^+ \rightarrow \bar{D}^{*0} D^{*0} K^+$
$B^0 \rightarrow \bar{D}^0 D^0 K^0$	$B^+ \rightarrow D^- D^+ K^+$
$B^0 \rightarrow \bar{D}^0 D^{*0} K^0 + \bar{D}^{*0} D^0 K^0$	$B^+ \rightarrow D^- D^{*+} K^+$
	$B^+ \rightarrow D^{*-} D^+ K^+$
$B^0 \rightarrow \bar{D}^{*0} D^{*0} K^0$	$B^+ \rightarrow D^{*-} D^{*+} K^+$

# The $D_{s1}(2700)$

- The  $D_{s1}(2700)$  was **discovered** by BaBar in inclusive  $e^+e^-$  interactions
  - Decaying to DK
  - Observed later also in  $D^*K$
  - Discovered as well  $D_{sJ}(2860)$  and  $D_{sJ}(3040)$

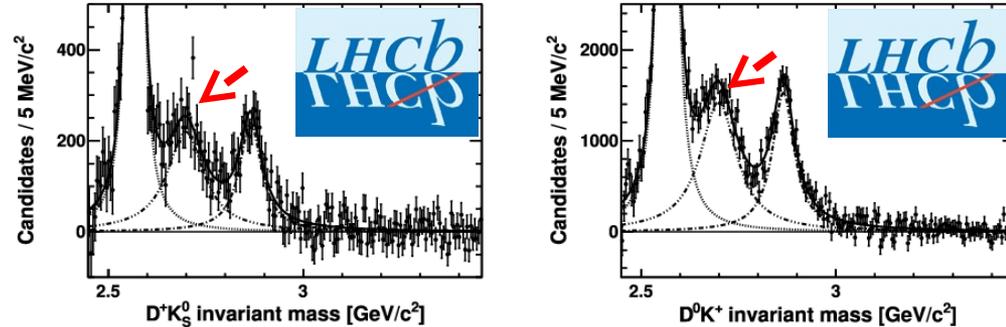


This discovery was **confirmed by Belle** in  $B^+ \rightarrow \bar{D}^0(D^0K^+)$



# The $D_{s1}(2700)$ , continued

- LHCb also studied this state with  $1.0 \text{ fb}^{-1}$  R. Aaij *et al.*, JHEP 1210 (2012) 151



- Found properties:

Name	$J^P$	Mass ( $\text{MeV}/c^2$ )	Width (MeV)
$D_{s1}^*(2700)$ (PDG)	$1^-$	$2709 \pm 4$	$117 \pm 13$

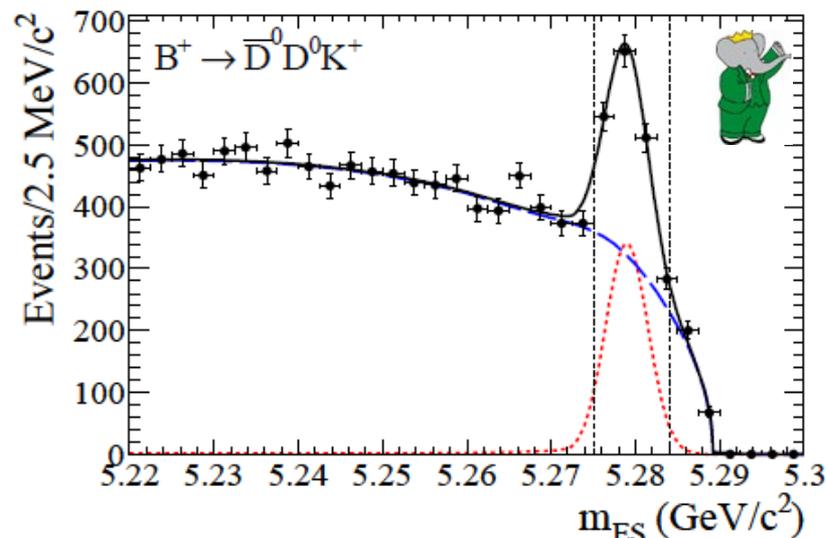
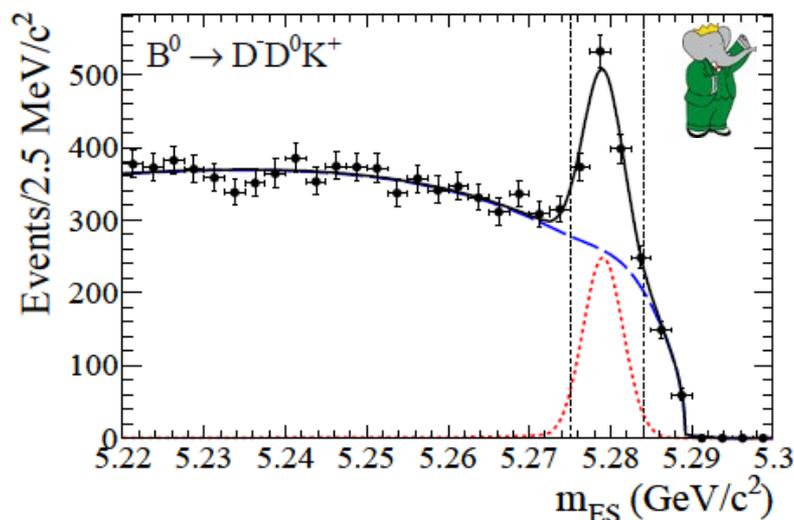
- Our goal here is to study the  $D_{s1}(2700)$  using a full Dalitz analysis
- We use both  $B^0 \rightarrow D^- D^0 K^+$  and  $B^+ \rightarrow \bar{D}^0 D^0 K^+$  channels
  - We do not attempt to study channels containing  $D^*$  mesons (vector)

# The Data Sample

- Run1-Run6, 429 fb<sup>-1</sup>:  $N_{\text{BB}^-} = (470.9 \pm 0.1 \pm 2.8) \times 10^6$
- Exclusive reconstruction
  - $D^0 \rightarrow K^- \pi^+$ ,  $D^0 \rightarrow K^- \pi^+ \pi^0$ ,  $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$
  - $D^+ \rightarrow K^- \pi^+ \pi^+$
  - For  $\bar{D}^0 D^0 K^+$ , at least one of the  $D^0$ 's is required to decay to  $K^- \pi^+$
- Use the exact same selection as the analysis on the measurement of 22 branching fractions
  - Based on track quality, Particle ID
  - Invariant  $D$  mass
  - Topological variables
  - $\Delta E$  cut

# The Data Sample, continued

- $m_{ES}$  distribution after the complete selection



- To obtain the Dalitz plot, a cut on  $m_{ES}$  is also imposed
- $B^0 \rightarrow D^- D^0 K^+$ : 1470 events with a purity of  $(38.6 \pm 2.8 \pm 2.1)\%$
- $B^+ \rightarrow \bar{D}^0 D^0 K^+$ : 1894 events with a purity of  $(41.6 \pm 2.5 \pm 3.1)\%$

# Dalitz Plot Analysis

- **Isobar formalism**  $\mathcal{M} = \sum_i c_i A_i$ 
  - $c_i$ : complex coefficients representing the **modulus** and **phase**
  - $A_i$ : complex amplitudes representing the **dynamical function** describing the **intermediate resonance**

- **Likelihood**

$$\mathcal{L} = p \times \varepsilon(m_1^2, m_2^2) \times \frac{|\mathcal{M}|^2}{\int |\mathcal{M}|^2 \varepsilon(m_1^2, m_2^2) dm_1^2 dm_2^2} + (1 - p) \times \frac{B(m_1^2, m_2^2)}{\int B(m_1^2, m_2^2) dm_1^2 dm_2^2}$$

- $p$ : **purity** from  $m_{ES}$  fits
- $\varepsilon$  is the **efficiency** and  $B$  the **background** in the Dalitz plane

- **Minimizing**

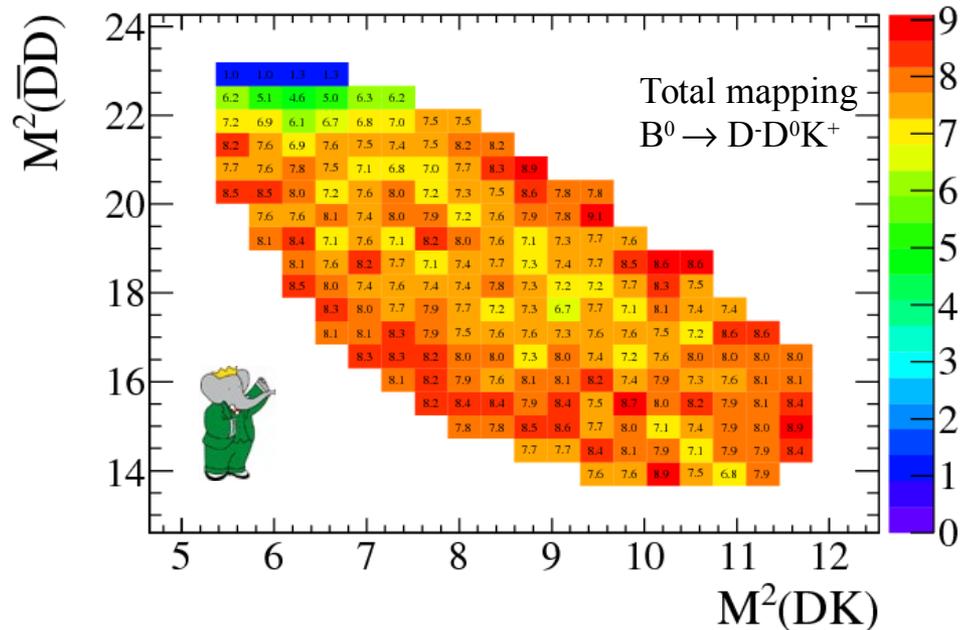
$$\mathcal{F} = \sum_i -2 \times \log(\mathcal{L}_i)$$

- To compare fits we use

$$\Delta\mathcal{F} = \mathcal{F} - \mathcal{F}_{\text{nominal}}$$

# Efficiency across the Plot

- Efficiency determined from flat-distribution simulated Dalitz in each D submode
  - 22×22 bins
- Overall efficiency obtained by weighting all D submodes by their Branching Fractions (Bfs)
- Bins are combined if <10 events in the bin
- **2D-Interpolation** of the binned efficiencies gives efficiency at any point
- At edge of plot do not use interpolation



# Background Term in the Fits

- From generic MC with the same selections as the data
  - We checked using the  $m_{ES}$  sideband that the MC correctly reproduces the data
- Histogram the background Dalitz plot (30x30 bins)
  - Non-uniform distribution: no fit done (not expected to fit well)
- Use a 2D-interpolation of the distribution, just as for efficiency

# Dalitz Plots

## ● Expected contributions

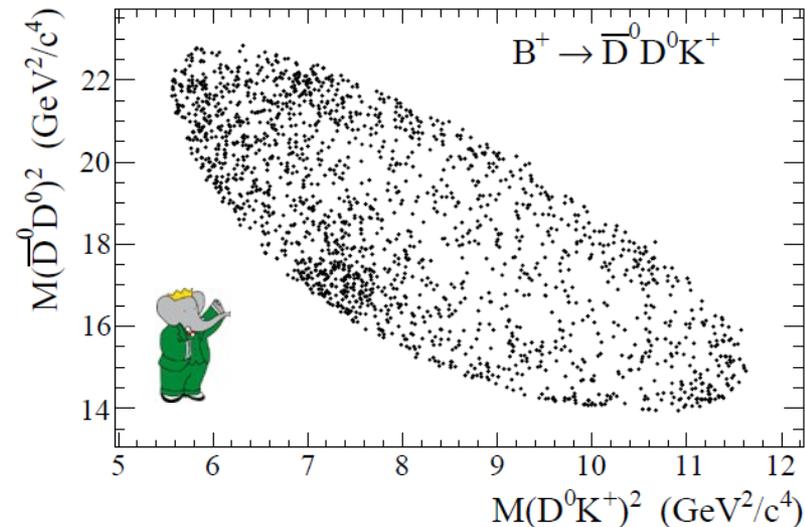
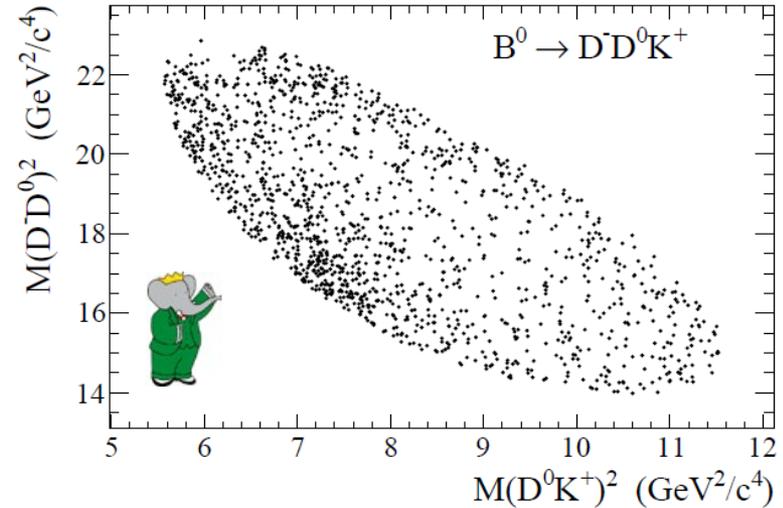
- Nonresonant events
- $D_{s1}(2700) \rightarrow D^0 K^+$
- $D_{s2}^*(2573) \rightarrow D^0 K^+$ 
  - Has never been observed in DDK
- $D_{sJ}^*(2860) \rightarrow D^0 K^+$ 
  - Not included in the nominal fit

## ● Additional contributions for $\bar{D}^0 D^0 K^+$

- $\psi(3700) \rightarrow \bar{D}^0 D^0$
- $\psi(4160) \rightarrow \bar{D}^0 D^0$
- $\chi_{c2}(2P)$ ,  $\psi(4040)$ ,  $\psi(4415)$  also possible, not included in the nominal fit

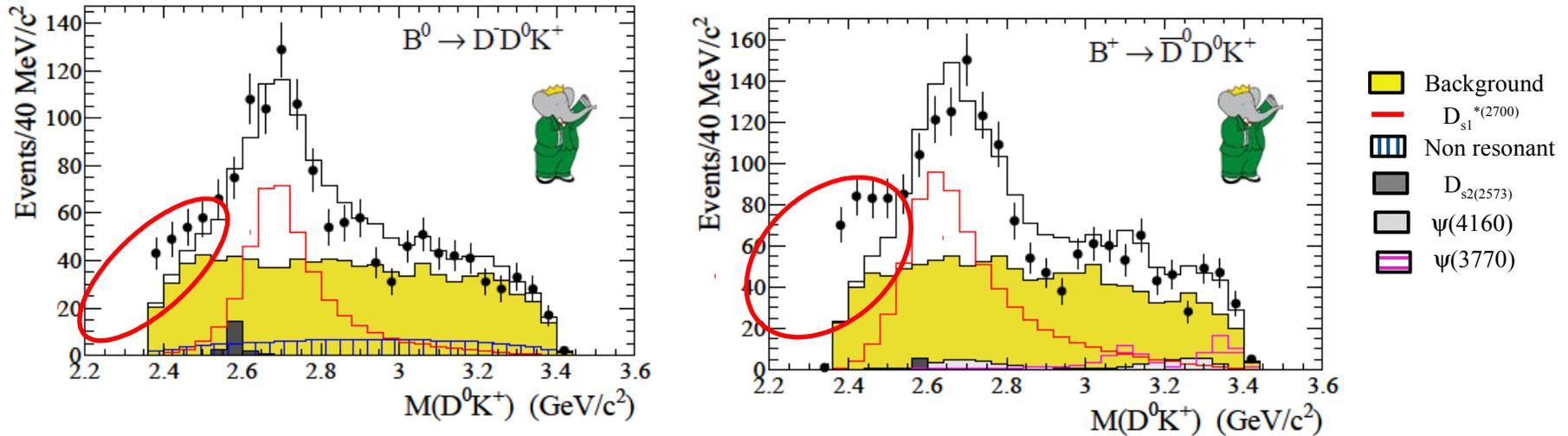
## ● All resonance parameters fixed to PDG, except $D_{s1}(2700)$ parameters

- $D_{s1}(2700)$  is the reference amplitude in the Dalitz fit



# Fits with known amplitudes

## ● Fits with known amplitudes



## ● Fits are not satisfactory

●  $B^0 \rightarrow D^-D^0K^+$ :  $\chi^2/\text{ndof} = 82/48$ ,  $\Delta F = 36$

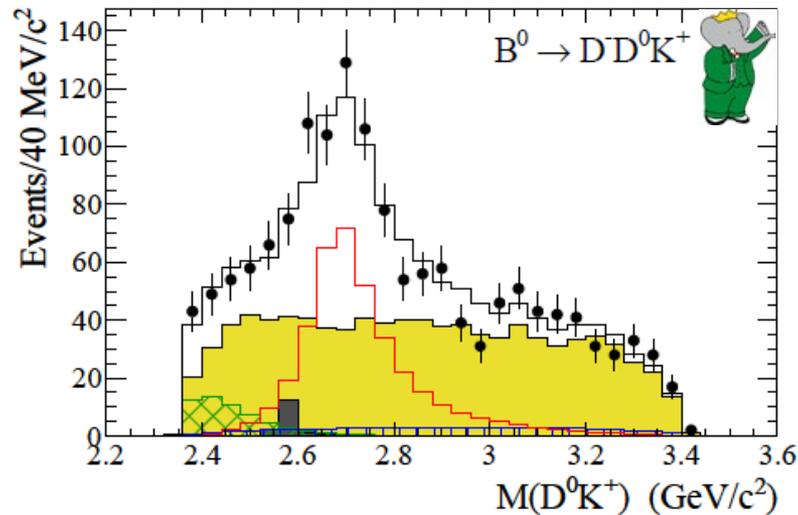
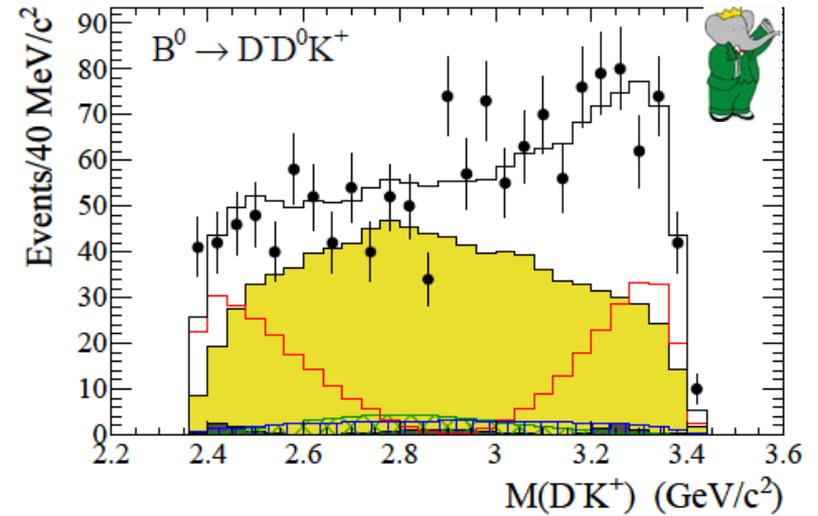
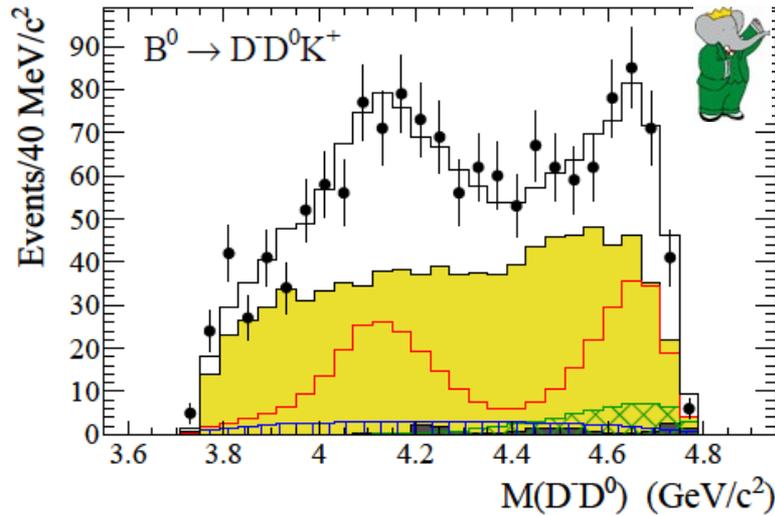
●  $B^+ \rightarrow \bar{D}^0D^0K^+$ :  $\chi^2/\text{ndof} = 265/51$ ,  $\Delta F = 223$

## ● Regions at low $D^0K^+$ mass not well described

# The Low Mass Effect

- Belle also observes this effect in  $B^+ \rightarrow \bar{D}^0 D^0 K^+$
- We checked that this contribution is from  $B \rightarrow DDK$  signal events and is not background
  - $m_{ES}$  binwise fits: fit  $m_{ES}$  in bins of  $m(D^0 K^+)$
  - sPlot
- We checked that this is not the reflection of a known resonance in another cross-feed mode
  - No contribution from  $D_{s1}(2536) \rightarrow D^* K$
  - No contribution from  $D_{s1}(2700) \rightarrow D(^*) K$
- Fits performed adding a scalar amplitude at low mass
  - Quality of fits improves
  - $B^0 \rightarrow D^- D^0 K^+$ :  $M_{\text{scalar}} = 2412 \pm 16 \text{ MeV}$ ,  $\Gamma_{\text{scalar}} = 163 \pm 64 \text{ MeV}$
  - $B^+ \rightarrow \bar{D}^0 D^0 K^+$ :  $M_{\text{scalar}} = 2453 \pm 20 \text{ MeV}$ ,  $\Gamma_{\text{scalar}} = 283 \pm 45 \text{ MeV}$
  - We reject this solution
    - Only  $\sim 1.5\sigma$  different
    - Such a wide resonance at this mass would be speculative
- It is not possible to conclude that a resonance contributes here
  - We use an arbitrary function to describe it
  - Exponential function  $A_{\text{ExpO}} = e^{-\alpha(m_2^2 - m_{2\text{thr}}^2)}$ 
    - (Some authors integrate this term into the nonresonant one)

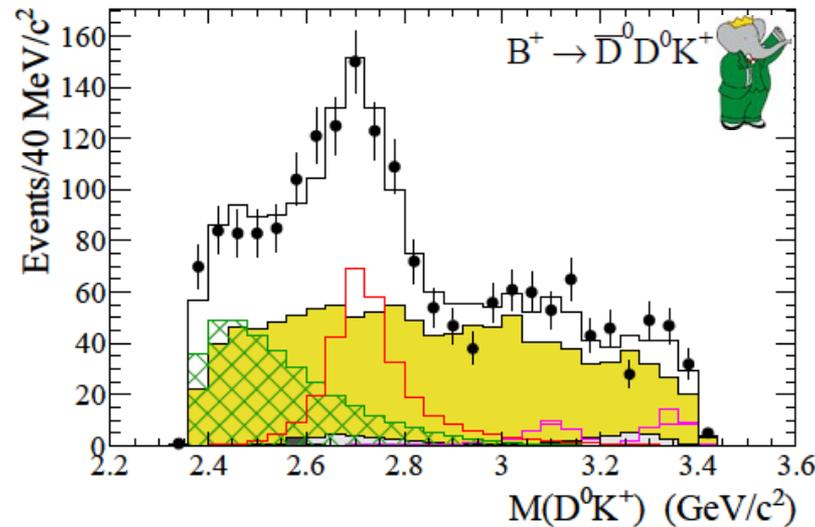
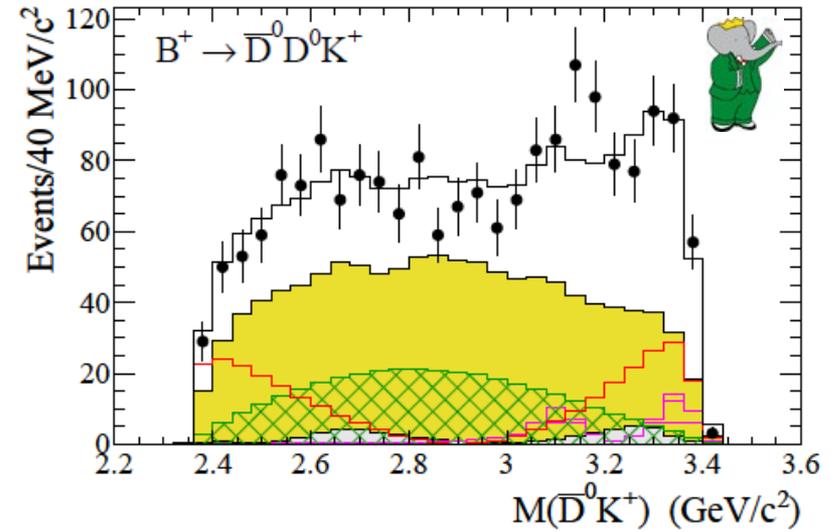
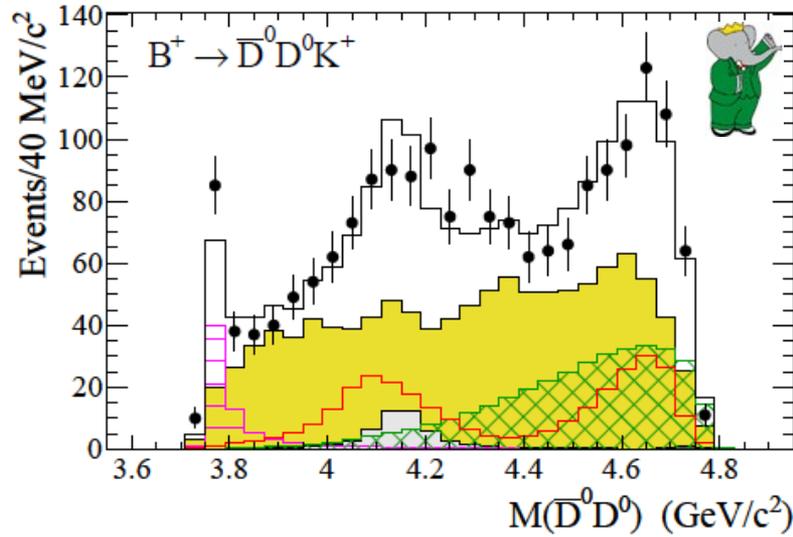
# The Nominal Fit: $B^0$



- Background
- $D_{s1}^*(2700)$
- Nonresonant
- $D_{s2}(2573)$
- Exponential

$$\chi^2/\text{ndof} = 56/45$$

# The Nominal Fit: $B^+$



- Background
- $D_{s1}^*(2700)$
- $D_{s2}(2573)$
- $\psi(4160)$
- $\psi(3770)$
- Exponential

$$\chi^2/\text{ndof} = 86/48$$

# Nominal Fits, continued

- Each fit result is in fact the **best fit** among 250; these use **randomized** initial parameters [within their bounds].
  - Choose the **smallest negative log likelihood**
  - Avoids **local minima** (as opposed to the global minimum)
- We reject **nonconverging fits** + fits with fit fraction sum > 250%
  - Due to the **unusually large interference** between the exponential and the non-resonant components for  $B^0 \rightarrow D^- D^0 K^+$
- We include in the **systematics** the small differences in the resonance parameters for the fits **close to the minimum**
- The presence of several close minima is confirmed **by toy MC**

# Systematic Effects

- Fit bias
  - Generate **toy MC samples** using the fit parameters and fit these toys to extract the fit bias
- Efficiency
  - **Raw efficiency** instead of interpolation
  - **Statistical fluctuation** taken into account by randomizing (within stat. uncertainty) the efficiency in each bin
- Background description
  - **Signal purity** varied according to its total uncertainty
- Fit model
  - **Blatt-Weisskopf** factor varied from 0 to 5 GeV<sup>-1</sup> (nominal 1.5 GeV<sup>-1</sup>)
  - **Low-mass effect**: use a scalar fit or an alternative arbitrary function
  - **$\psi(3770)$** : using KEDR exp. results instead of PDG values
  - **D<sub>s2</sub>(2573)**: fit repeated without this (small) contribution
- Local minima
  - Use the **other** minima (close enough to the global one)

# Estimates of Systematic errors

Units are MeV/c<sup>2</sup> (for M), MeV (for  $\Gamma$ )

- **Breakdown** of systematic errors on the  $D_{s1}(2700)$  parameters

$$B^0 \rightarrow D\bar{D}^0 K^+$$

Parameter	Value	Bias	Eff.	Eff. II	Bkg	BW	Low mass	$D_{s2}^*$	Min.	Total
$M(D_{s1}^*(2700)^+)$	2694	$\pm 2$	0	$\pm 1$	0	$\begin{smallmatrix} +13 \\ -2 \end{smallmatrix}$	$\begin{smallmatrix} +0 \\ -1 \end{smallmatrix}$	0	$\begin{smallmatrix} +3 \\ 0 \end{smallmatrix}$	$\begin{smallmatrix} +13 \\ -3 \end{smallmatrix}$
$\Gamma(D_{s1}^*(2700)^+)$	145	$\pm 8$	$\pm 1$	$\pm 3$	$\begin{smallmatrix} +4 \\ -3 \end{smallmatrix}$	$\begin{smallmatrix} +17 \\ -9 \end{smallmatrix}$	$\begin{smallmatrix} +5 \\ -0 \end{smallmatrix}$	-6	$\begin{smallmatrix} +11 \\ -4 \end{smallmatrix}$	$\begin{smallmatrix} +22 \\ -14 \end{smallmatrix}$

$$B^+ \rightarrow \bar{D}^0 D^0 K^+$$

Parameter	Value	Bias	Eff.	Eff. II	Bkg	BW	Low mass	$D_{s2}^*$	$\psi$	Min.	Total
$M(D_{s1}^*(2700)^+)$	2707	$\pm 4$	0	$\pm 1$	$\pm 3$	$\begin{smallmatrix} +7 \\ -4 \end{smallmatrix}$	$\begin{smallmatrix} +0 \\ -4 \end{smallmatrix}$	+1	0	$\begin{smallmatrix} +0 \\ -5 \end{smallmatrix}$	$\pm 8$
$\Gamma(D_{s1}^*(2700)^+)$	113	$\pm 5$	$\pm 1$	$\pm 3$	$\begin{smallmatrix} +9 \\ -7 \end{smallmatrix}$	$\begin{smallmatrix} +17 \\ -0 \end{smallmatrix}$	$\begin{smallmatrix} +0 \\ -9 \end{smallmatrix}$	-5	+2	$\begin{smallmatrix} +0 \\ -7 \end{smallmatrix}$	$\begin{smallmatrix} +20 \\ -16 \end{smallmatrix}$

# Results

- $D_{s1}(2700)$  observed for the first time in  $B^0 \rightarrow D^- D^0 K^+$  decays
- Low-mass effect has an important contribution
- $D_{s2}(2573)$  observed with a  $3.4\sigma$  significance (including systematics) in  $B^0 \rightarrow D^- D^0 K^+$
- $\psi(4160)$  observed with a  $3.3\sigma$  significance (including systematics) in  $B^+ \rightarrow D^0 D^0 K^+$
- No need for  $D_{sJ}^*(2860)$ ,  $D_{sJ}(3040)$ ,  $\chi_{c2}(2P)$ ,  $\psi(4040)$ ,  $\psi(4415)$

$$B^0 \rightarrow D^- D^0 K^+$$

Contribution	Modulus	Phase ( $^\circ$ )	Fraction (%)
$D_{s1}^*(2700)^+$	1.00	0	$66.7 \pm 7.8^{+3.5}_{-3.8}$
$D_{s2}^*(2573)^+$	$0.031 \pm 0.008 \pm 0.002$	$277 \pm 17^{+6}_{-9}$	$3.2 \pm 1.6^{+0.3}_{-0.4}$
Nonresonant	$1.33 \pm 0.63^{+0.46}_{-0.35}$	$287 \pm 21^{+10}_{-15}$	$10.9 \pm 6.6^{+7.0}_{-4.3}$
Exponential	$6.94 \pm 1.83^{+0.82}_{-0.43}$	$269 \pm 33^{+17}_{-15}$	$9.9 \pm 2.9^{+3.0}_{-3.3}$
Sum			$90.6 \pm 10.7^{+8.4}_{-6.7}$

$$B^+ \rightarrow \bar{D}^0 D^0 K^+$$

Contribution	Modulus	Phase ( $^\circ$ )	Fraction (%)
$D_{s1}^*(2700)^+$	1.00	0	$38.3 \pm 5.0^{+0.8}_{-6.2}$
$D_{s2}^*(2573)^+$	$0.021 \pm 0.010^{+0.009}_{-0.003}$	$267 \pm 30^{+17}_{-13}$	$0.6 \pm 1.1^{+0.4}_{-0.2}$
$\psi(3770)$	$1.40 \pm 0.21^{+0.20}_{-0.24}$	$284 \pm 22^{+26}_{-30}$	$9.0 \pm 3.1^{+0.4}_{-0.8}$
$\psi(4160)$	$0.78 \pm 0.20^{+0.18}_{-0.14}$	$188 \pm 13^{+14}_{-17}$	$6.4 \pm 3.1^{+1.9}_{-2.4}$
Exponential	$16.15 \pm 2.26^{+1.09}_{-1.74}$	$308 \pm 8^{+6}_{-5}$	$44.5 \pm 6.2^{+1.3}_{-2.1}$
Sum			$98.9 \pm 9.2^{+2.5}_{-7.0}$

# Branching Fractions

- We measure the partial branching fractions of the resonances
- We use  $f_{\text{res}}$ , the fit fraction of the resonance and  $B_{\text{tot}}$ , the total branching fraction of the mode measured in our previous publication

$$\mathcal{B}_{\text{res}} = f_{\text{res}} \times \mathcal{B}_{\text{tot}}$$

Mode	$\mathcal{B} (10^{-4})$
$B^0 \rightarrow D^- D_{s1}^* (2700)^+ [D^0 K^+]$	$7.14 \pm 0.96 \pm 0.69$
$B^+ \rightarrow \bar{D}^0 D_{s1}^* (2700)^+ [D^0 K^+]$	$5.02 \pm 0.71 \pm 0.93$
$B^0 \rightarrow D^- D_{s2}^* (2573)^+ [D^0 K^+]$	$0.34 \pm 0.17 \pm 0.05$
$B^+ \rightarrow \bar{D}^0 D_{s2}^* (2573)^+ [D^0 K^+]$	$0.08 \pm 0.14 \pm 0.05$
$B^+ \rightarrow \psi(3770) K^+ [\bar{D}^0 D^0]$	$1.18 \pm 0.41 \pm 0.15$
$B^+ \rightarrow \psi(4160) K^+ [\bar{D}^0 D^0]$	$0.84 \pm 0.41 \pm 0.33$

# $D_{s1}(2700)$ results

- Mass and width of the  $D_{s1}(2700)$  for the two modes

Mode	Mass (MeV/ $c^2$ )	Width (MeV)
$B^0 \rightarrow D^- D^0 K^+$	$2694 \pm 8^{+13}_{-3}$	$145 \pm 24^{+22}_{-14}$
$B^+ \rightarrow \bar{D}^0 D^0 K^+$	$2707 \pm 8 \pm 8$	$113 \pm 21^{+20}_{-16}$

- The two modes are **in agreement** within their uncertainties
- The two measurements are combined by computing a **weighted mean** taking into account the asymmetric uncertainties; this works well for all **uncorrelated** uncertainties. The Blatt-Weisskopf factor uncertainties are *correlated*, so these are removed from the combination, and taken accounted for later in a conservative fashion.

# $D_{s1}(2700)$ results, continued

- Mass and width after **combining modes** (with total uncertainties)

$$M(D_{s1}^*(2700)^+) = 2699_{-7}^{+14} \text{ MeV}/c^2,$$

$$\Gamma(D_{s1}^*(2700)^+) = 127_{-19}^{+24} \text{ MeV},$$



- **Compatible** with the world average

$$M(D_{s1}^*(2700)^+) = 2709 \pm 4 \text{ MeV}/c^2$$

$$\Gamma(D_{s1}^*(2700)^+) = 117 \pm 13 \text{ MeV}$$

- **Spin** of  $D_{s1}(2700)$

- Analysis performed with  $J = 1$
- Fits repeated with  $J = 0$  and  $J = 2$

Mode	$J = 0$		$J = 1$		$J = 2$	
	$\Delta\mathcal{F}$	$\chi^2/n_{\text{dof}}$	$\chi^2/n_{\text{dof}}$	$\Delta\mathcal{F}$	$\chi^2/n_{\text{dof}}$	
$B^0 \rightarrow D^- D^0 K^+$	131	131/45	<b>56/45</b>	108	125/45	
$B^+ \rightarrow \bar{D}^0 D^0 K^+$	63	137/48	<b>86/48</b>	99	145/48	

- Assuming parity conservation, we deduce  $D_{s1}(2700)$  is a  $1^-$  state

# Conclusions

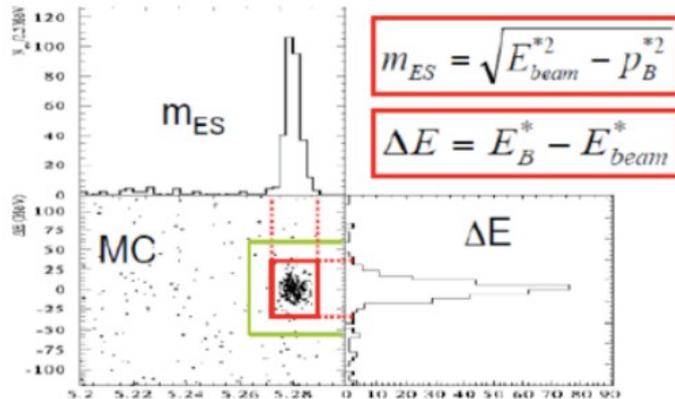


- We performed a Dalitz analysis of the modes  $B^0 \rightarrow D^- D^0 K^+$  and  $B^+ \rightarrow \bar{D}^0 D^0 K^+$ 
  - We extract moduli and phases for all contributions
- We observe the  $D_{s1}(2700)$  meson in both final states
  - We measure precisely its **mass and width**
- We observe an **enhancement** between 2350 and 2500 MeV in the  $D^0 K^+$  invariant mass
  - We are **not able** to interpret this effect
  - It is described in the fit by an **ad-hoc function**
  - Could be a **new  $D_s$**  excited state?
  - A specific form of a **nonresonant amplitude**?
  - More information will be brought by **LHCb** and **Belle II**
- We do not observe the  $D_{sJ}(2860)$  and  $D_{sJ}(3040)$  in these final states

# ADDITIONAL SLIDES

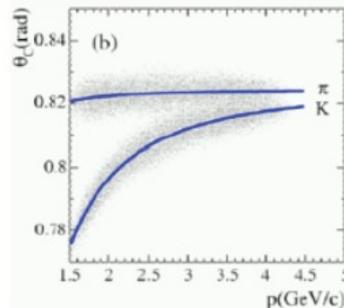
# Common analysis techniques

## Kinematics of fully reconstructed B



## K/ $\pi$ separation

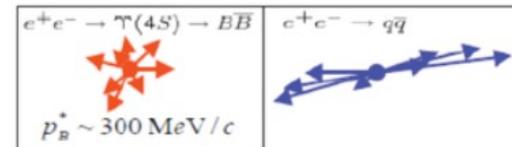
Very good particle ID between 1.5 and 4 GeV/c



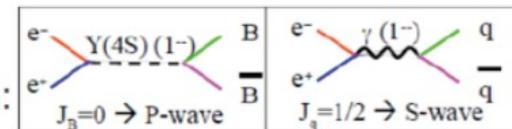
## Background discrimination

Suppression by multi-variable classifiers based on event-shape variables: Fisher discriminant, Boosted Decision Trees (BTD)...

Topology:



Angular distribution:



- Strongly discriminate continuum events ( $e^+e^- \rightarrow q\bar{q}$  ( $q = u, d, s, c$ ))
- Background from B decays

Variables are often combined to a likelihood function, used in a maximum likelihood fit for signal/background separation and to measure parameters of interest

# EVENT SELECTION

<b>Selection for the primary charged <math>K</math></b>	<b>Selection for the primary neutral <math>K</math></b>
1 - GoodTrackLoose + KLHNotAPion 2 - KLHTight	1 - $ M(K_s^0) - M(K_s^0)_{PDG}  < 9.5 \text{ MeV}/c^2$ + $p(\chi^2) > 0.1\%$ + Length of flight $> 2 \text{ mm}$
<b>Selection for <math>D^0 \rightarrow K^- \pi^+</math></b>	<b>Selection for <math>D^0 \rightarrow K^- \pi^+ \pi^0</math></b>
1 - $ M(D^0) - M(D^0)_{Meas.}  < 2.5\sigma$ + $K$ KLHNotAPion + $p(\chi^2) > 0.1\%$ 2 - $K$ KLHTight	1 - $ M(D^0) - M(D^0)_{Meas.}  < 2.5\sigma$ + $K$ KLHNotAPion + $p(\chi^2) > 0.1\%$ 2 - $K$ KLHTight 3 - Dalitz weight $> 10$
<b>Selection for <math>D^0 \rightarrow K^- \pi^+ \pi^- \pi^+</math></b>	<b>Selection for <math>D^+ \rightarrow K^- \pi^+ \pi^+</math></b>
1 - $ M(D^0) - M(D^0)_{Meas.}  < 2.5\sigma$ + $K$ KLHNotAPion + $p(\chi^2) > 0.1\%$ 2 - $K$ KLHTight	1 - $ M(D^+) - M(D^+)_{Meas.}  < 2.5\sigma$ + $K$ KLHNotAPion + $p(\chi^2) > 0.1\%$ 2 - $K$ KLHTight
<b>Selection for <math>D^{*+} \rightarrow D^0 \pi^+, D^+ \pi^0</math></b>	<b>Selection for <math>D^{*0} \rightarrow D^0 \pi^0, D^0 \gamma</math></b>
1 - $ \Delta M - \Delta M_{PDG}  < 3 \text{ MeV}/c^2$ where $\Delta M = M(D^{*+}) - M(D^0/D^+)$ + $p^*(\pi) < 450 \text{ MeV}/c$ + $D^0/D^+$ selection steps described above	1 - $\Delta M \in [138, 146] (D^0 \pi^0), [130, 150] (D^0 \gamma) \text{ MeV}/c^2$ where $\Delta M = M(D^{*0}) - M(D^0)$ + $p^*(\pi^0) < 450 \text{ MeV}/c + E(\gamma) > 100 \text{ MeV}$ + $D^0$ selection steps described above
<b>Selection for <math>B</math></b>	<b>Final step</b>
1 - $D^{(*)}$ and $K$ at least satisfying the level of selection 1 described above + $R_2 < 0.3$ + $ \cos(\theta_B)  < 0.9$	1 - Best $\Delta E$ candidate + $\Delta E$ cut (see Table 5 of BAD 2141) + $m_{ES}$ cut (see text)